

1

(canonical approach still): Given eq. 130.1 (in the notes), and the properties of a , b , u and v , obtain the Feynman propagator for fermions:

$$S_F(x-y) \equiv \langle 0 | T \{ \psi(x) \bar{\psi}(y) \} | 0 \rangle = \int \frac{d^4 p}{(2\pi)^4} \frac{i(\not{p} + m) e^{-i p(x-y)}}{p^2 - m^2 + i\epsilon}$$

(attention to the time ordering for fermions:)

$$T \{ \psi(x) \bar{\psi}(y) \} = \begin{cases} \psi(x) \bar{\psi}(y) & x^0 > y^0 \\ -\bar{\psi}(y) \psi(x) & y^0 > x^0 \end{cases}$$

2

(In the context of pg 133 of the lecture notes) show that:

$$\frac{\partial}{\partial \theta_k} e^{\sum \theta_i \eta_i} = \eta_k e^{\sum \theta_i \eta_i} \quad \frac{\partial}{\partial \eta_k} e^{\sum \theta_i \eta_i} = -\theta_k e^{\sum \theta_i \eta_i}$$

3

In analogy to what we did for the bosonic harmonic oscillator, obtain eq 138.3 of the lecture notes